

Blue: Writing and Graphing Inequalities

Name _____

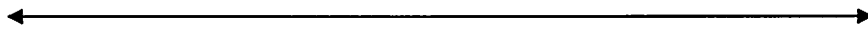
1. a) That package must weigh at least 100 pounds!



- b) All of the fish in the tank have more than 20 spots but at most 50 spots



- c) $[-3, 9]$

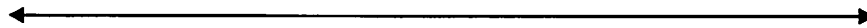


Name _____

2. a) The water temperature is less than 60 degrees.



- b) I want my newborn to have a name that's at least 4 letters long but no more than 8 letters.

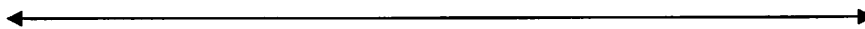


- c) $(5, 7]$



Name_____ -

3. a) Joe has more than 7 cousins



- b) You better get a grade between 80 and 100 inclusively on the next test.



- c) $(-4, 0)$



Name_____

4. a) I've got no more than \$50 in my pocket.



- b) Jeremy walks more than 4 miles but less than 8 miles every week.



- c) $[7, 10)$

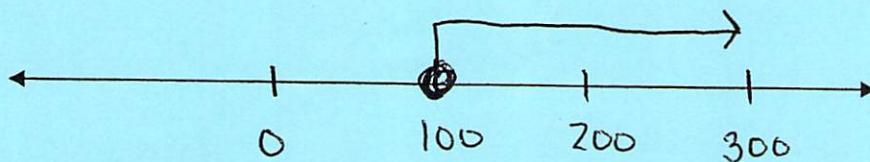


Blue: Writing and Graphing Inequalities

Name Key

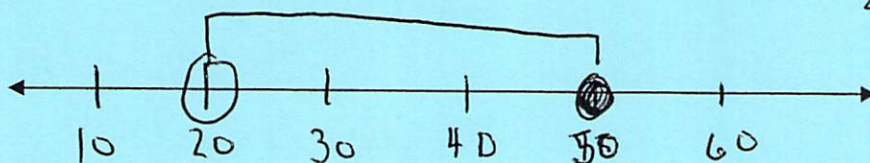
1. a) That package must weigh at least 100 pounds!

$$x \geq 100$$



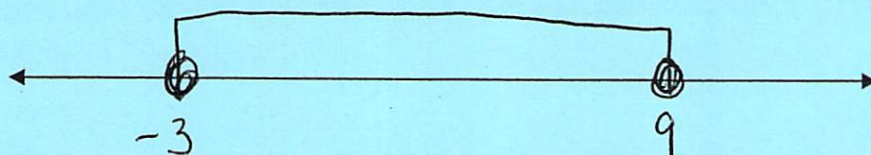
- b) All of the fish in the tank have more than 20 spots but at most 50 spots

$$20 < x \leq 50$$



- c) $[-3, 9]$

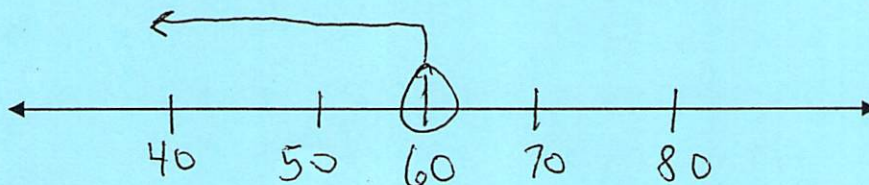
$$-3 \leq x \leq 9$$



Name Key

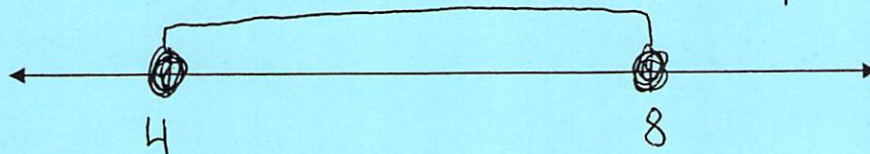
2. a) The water temperature is less than 60 degrees.

$$x < 60$$



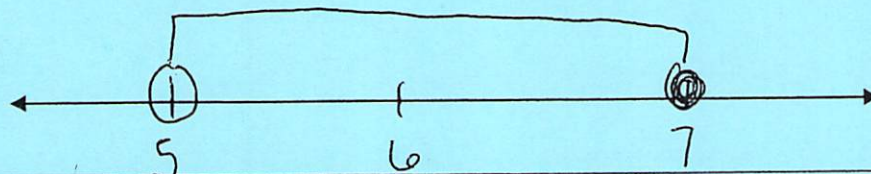
- b) I want my newborn to have a name that's at least 4 letters long but no more than 8 letters.

$$4 \leq x \leq 8$$



- c) $[5, 7]$

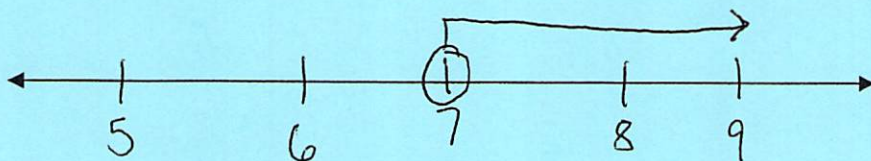
$$5 \leq x \leq 7$$



Name Key

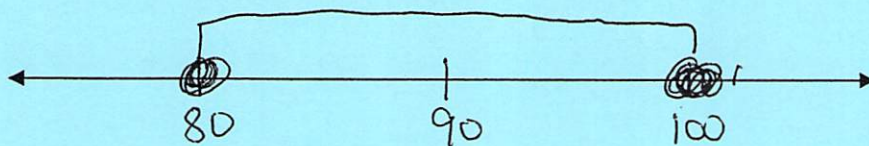
3. a) Joe has more than 7 cousins

$$x > 7$$



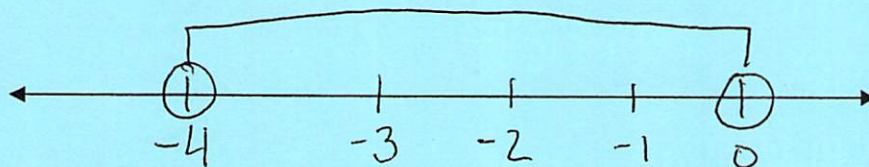
- b) You better get a grade between 80 and 100 inclusively on the next test.

$$80 \leq x \leq 100$$



- c) $(-4, 0)$

$$-4 < x < 0$$



Name Key

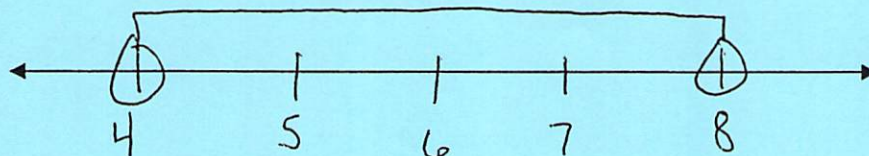
4. a) I've got no more than \$50 in my pocket.

$$x \leq 50$$



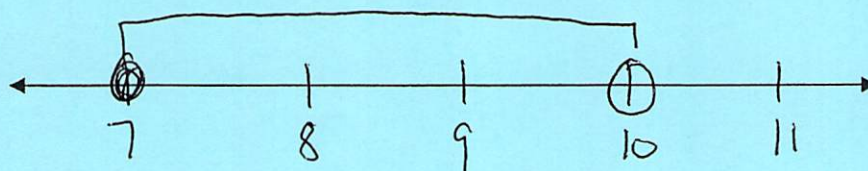
- b) Jeremy walks more than 4 miles but less than 8 miles every week.

$$4 < x < 8$$



- c) $[7, 10)$

$$7 \leq x < 10$$



Green: Solving Inequalities

Name _____

1. (a) Which of the following is a solution to the inequality: $-2x + 5 > 11$

(1) 4 (2) 0 (3) -3 (4) -5

- (b) Which of the following is **NOT** a solution to the inequality: $-\frac{x}{7} \geq -3$

(1) 21 (2) 20 (3) -21 (4) 24

Name _____

2. (a) Which of the following is **NOT** a solution to the inequality: $-7x + 9 \leq -19$

(1) -4 (2) 4 (3) 5 (4) 6

- (b) Which of the following is a solution to the inequality: $-\frac{x}{2} > 5$

(2) 10 (2) -10 (3) -15 (4) 15

<p>3. (a) <u>Name</u> Which of the following is a solution to the inequality:</p> <p>$-4x + 3 < -1$</p> <p>(1) -1 (2) 1 (3) -2 (4) 2</p> <p>(b) Which of the following is NOT a solution to the inequality:</p> <p>$-\frac{x}{6} \leq 1$</p> <p>(1) -6 (2) 20 (3) 35 (4) -24</p>	<p>4. (a) <u>Name</u> Which of the following is NOT a solution to the inequality:</p> <p>$-x + 6 \leq 3$</p> <p>(2) 3 (2) -3 (3) 4 (4) 25</p> <p>(b) Which of the following is NOT a solution to the inequality:</p> <p>$-\frac{x}{8} > -5$</p> <p>(2) 38 (2) 39 (3) -40 (4) 41</p>
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Green: Solving Inequalities

Name Key

1. (a) Which of the following is a solution to the inequality:

$$\begin{array}{r} -2x + 5 > 11 \\ -5 \quad -5 \\ \hline -2x > 6 \\ \frac{-2x}{-2} > \frac{6}{-2} \\ x < -3 \end{array}$$

(1) 4

(2) 0

(3) -3

(4) -5

- (b) Which of the following is **NOT** a solution to the inequality: $-7 \cdot -\frac{x}{7} \geq -3 \cdot -7$

(1) 21

(2) 20

(3) -21

(4) 24

$$x \leq 21$$

Name Key

2. (a) Which of the following is **NOT** a solution to the inequality:

$$\begin{array}{r} -7x + 9 \leq -19 \\ -9 \quad -9 \\ \hline -7x \leq -28 \\ \frac{-7x}{-7} \leq \frac{-28}{-7} \\ x \geq 4 \end{array}$$

(1) -4

(2) 4

(3) 5

(4) 6

- (b) Which of the following is a solution to the inequality: $-2 \cdot -\frac{x}{2} > 5 \cdot -2$

(2) 10

(2) -10

(3) -15

(4) 15

$$x < -10$$

Name Key

3. (a) Which of the following is a solution to the inequality:

$$\begin{array}{r} -4x + 3 < -1 \\ -3 \quad -3 \\ \hline -4x < -4 \\ \hline -4 \quad -4 \\ \hline \end{array}$$

$$x > 1$$

(1) -1

(2) 1

(3) -2

(4) 2

(b) Which of the following is **NOT** a solution to the inequality: $-6 \cdot -\frac{x}{6} \leq 1 \cdot -6$

$$x \geq -6$$

(1) -6

(2) 20

(3) 35

(4) -24

Name Key

4. (a) Which of the following is **NOT** a solution to the inequality:

$$\begin{array}{r} -x + 6 \leq 3 \\ -6 \quad -6 \\ \hline \end{array}$$

$$\begin{array}{r} -x \leq -3 \\ -1 \quad -1 \\ \hline \end{array}$$

$$x \geq 3$$

(2) 3

(2) -3

(3) 4

(4) 25

(b) Which of the following is **NOT** a solution to the inequality: $-8 \cdot -\frac{x}{8} > -5 \cdot -8$

$$x < 40$$

(2) 38

(2) 39

(3) -40

(4) 41

Yellow: Multi-Step Inequalities

Name _____

1. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$5(-2 + x) < 3x + 2$$



Name _____

2. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

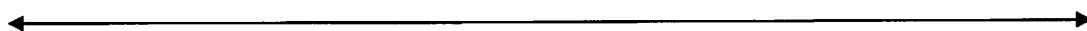
$$-7(x + 1) > -9 - 5x$$



Name_____

3. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$5 + 4x \geq x + 8$$



Name_____

4. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$-30 + 5x \leq 4(8x + 6)$$

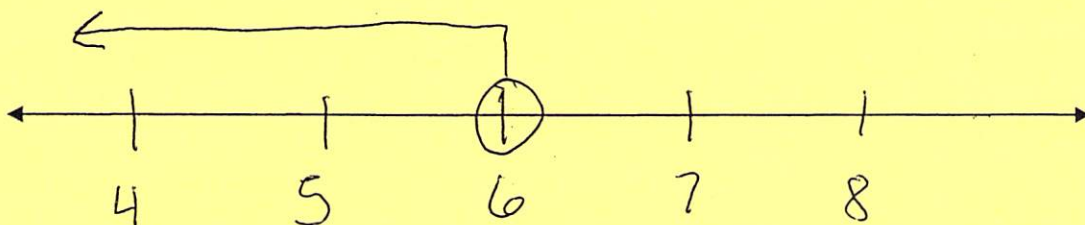


Yellow: Multi-Step Inequalities

Name Key

1. Solve and Graph your solution set.

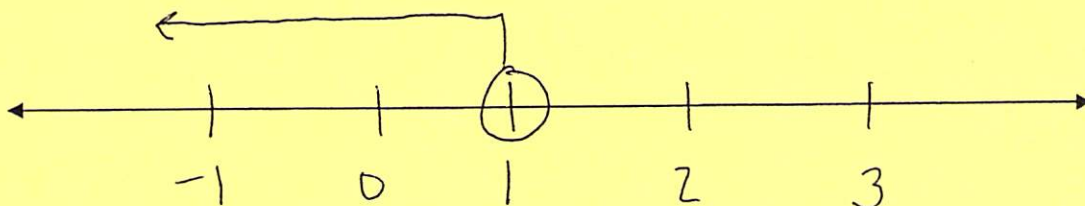
$$\begin{array}{rcl}
 5(-2+x) & < & 3x+2 \\
 -10 + 5x & < & 3x+2 \\
 +10 & & +10 \\
 \hline
 5x & < & 3x+12 \\
 -3x & & -3x \\
 \hline
 2x & < & 12 \\
 \frac{2x}{2} & < & \frac{12}{2} \\
 & & x < 6
 \end{array}$$



Name Key

2. Solve and Graph your solution set.

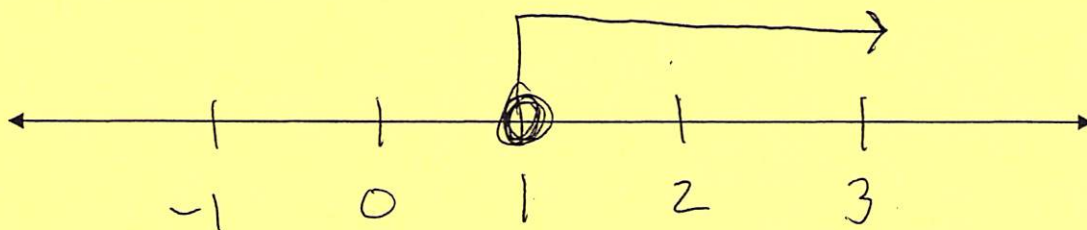
$$\begin{array}{rcl}
 -7(x+1) & > & -9-5x \\
 -7x-7 & > & -9-5x \\
 +7x & & +7x \\
 \hline
 -7 & > & -9+2x \\
 +9 & & +9 \\
 2 & > & 2x \\
 \frac{2}{2} & > & \frac{2x}{2} \\
 & & 1 > x \text{ or } x < 1
 \end{array}$$



Name Key

3. Solve and Graph your solution set.

$$\begin{array}{r|l}
 5 + 4x & \geq x + 8 \\
 -x & -x \\
 \hline
 5 + 3x & \geq 8 \\
 -5 & -5 \\
 \hline
 3x & \geq 3 \\
 \frac{3x}{3} & \frac{3}{3} \\
 x & \geq 1
 \end{array}$$

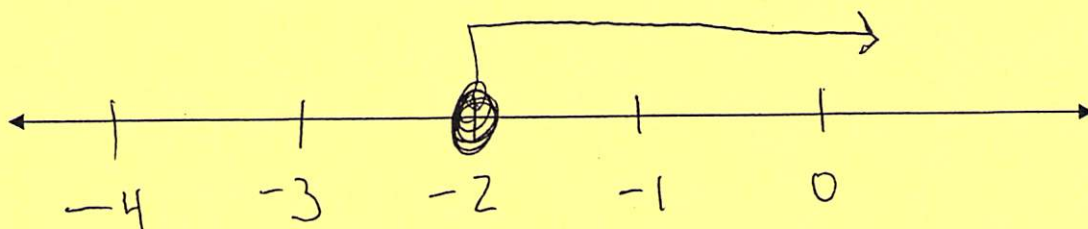


Name Key

4. Solve and Graph your solution set.

$$\begin{array}{r|l}
 -30 + 5x & \leq 4(8x + 6) \\
 -30 + 5x & \leq 32x + 24 \\
 -5x & -5x \\
 \hline
 -30 & \leq 27x + 24 \\
 -24 & -24 \\
 \hline
 -54 & \leq 27x \\
 \frac{-54}{27} & \frac{27x}{27} \\
 -2 & \leq x
 \end{array}$$

$-2 \leq x \text{ or } x \geq -2$



Pink: Inequalities Word Problems

Name _____

Write and Solve an Inequality

1. Leah estimates she needs \$165 to buy a new lacrosse stick. She has \$75 saved. Her father agreed to pay her \$8 an hour for gardening. What is the minimum number of hours Leah must work at gardening to earn \$165?

Name _____

Write and Solve an Inequality

2. Beth wanted to go to the school dance but only had \$25 to spend. If the ticket cost \$5 how many cookies could Beth buy at the dance if each cookie costs \$1.25?

Name _____

Write and Solve an Inequality

3. George wanted to start his own painting business. He bought a ladder and some supplies for \$180. He plans on charging \$10 per hour painting. How many hours will George have to work if he is to make at least a profit of \$750?

Name _____

Write and Solve an Inequality

4. Peter begins his kindergarten year able to spell 10 words. He is going to learn to spell 2 new words every day. Write an inequality to determine the minimum number of whole days it will take for him to be able to spell *at least* 75 words.

Pink: Inequalities Word Problems

Name Key

Write and Solve an Inequality

1. Leah estimates she needs \$165 to buy a new lacrosse stick. She has \$75 saved. Her father agreed to pay her \$8 an hour for gardening. What is the minimum number of hours Leah must work at gardening to earn \$165?

$$\begin{array}{r} 165 \leq 75 + 8h \\ -75 \quad -75 \\ \hline \end{array}$$

$$\frac{90}{8} \leq \frac{8h}{8}$$

$$11.25 \leq h$$

Let h = hours spent gardening

She must spend
12 hours gardening

Name _____

Write and Solve an Inequality

2. Beth wanted to go to the school dance but only had \$25 to spend. If the ticket cost \$5 how many cookies could Beth buy at the dance if each cookie costs \$1.25?

$$\begin{array}{r} 25 \geq 5 + 1.25c \\ -5 \quad -5 \end{array}$$

$$\frac{20}{1.25} \geq \frac{1.25c}{1.25}$$

$$16 \geq c$$

Let c = cookies bought

Beth can buy
16 cookies or less

Name _____

Write and Solve an Inequality

3. George wanted to start his own painting business. He bought a ladder and some supplies for \$180. He plans on charging \$10 per hour painting. How many hours will George have to work if he is to make at least a profit of \$750?

$$-180 + 10h \geq 750$$

$$\begin{array}{r} +180 \qquad \qquad +180 \\ \hline \end{array}$$

$$\frac{10h}{10} \geq \frac{930}{10}$$

$$h \geq 93$$

Let h = hours painting

George will have
to work 93
hours or more

Name _____

Write and Solve an Inequality

4. Peter begins his kindergarten year able to spell 10 words. He is going to learn to spell 2 new words every day. Write an inequality to determine the minimum number of whole days it will take for him to be able to spell *at least* 75 words.

$$\begin{array}{r} 10 + 2d \geq 75 \\ -10 \qquad \qquad -10 \end{array}$$

$$\frac{2d}{2} \geq \frac{65}{2}$$

$$d \geq 32.5$$

Let d = days of learning words

It will take Peter
at least 33 days

Purple: Compound Inequalities

Name _____

1. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$6 < \frac{-3(x + 7)}{4} \leq 18$$



Name _____

2. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$\frac{5x - 9}{4} > 2x \quad \text{or} \quad \frac{2}{3}x - 1 > 5$$



Name_____

3. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$-3 \leq \frac{1}{2}(x + 3) \leq 9$$



Name_____

4. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$4\frac{1}{5}x + 48 \leq x \quad \text{or} \quad \frac{x + 5}{4} < 2(x + 12)$$



Purple: Compound Inequalities

Name _____

1. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

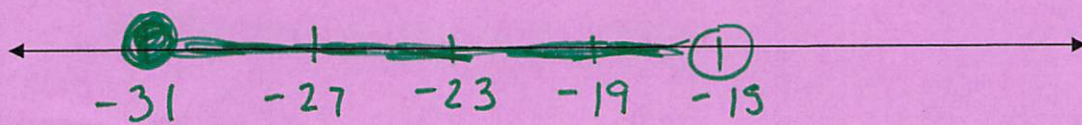
$$4 \cdot 6 < \frac{-3(x+7)}{4} \leq 18 \cdot 4$$

$$\frac{24}{-3} < \frac{-3(x+7)}{-3} \leq \frac{72}{-3}$$

$$\frac{-8}{-1} > \frac{x+7}{-1} \geq \frac{-24}{-1}$$

$$-15 > x \geq -31$$

$$[-31, -15)$$



Name _____

2. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$4 \cdot \frac{5x-9}{4} > 2x \cdot 4 \text{ or } \frac{2}{3}x - 1 > 5$$

$$\frac{5x-9}{-3} > \frac{8x}{-3}$$

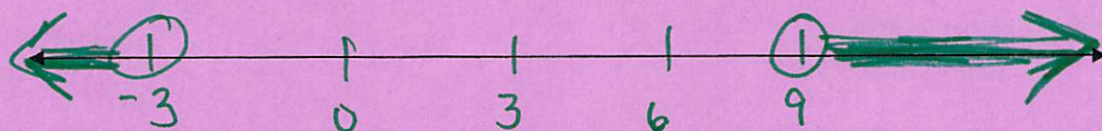
$$\frac{-9}{3} > \frac{3x}{3}$$

$$-3 > x$$

$$\frac{3}{2} \cdot \frac{2}{3}x > 6 \cdot \frac{3}{2}$$

$$\text{or } x > 9$$

$$(-\infty, -3) \cup (9, \infty)$$



Name _____

3. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$-3 \leq \frac{1}{2}(x+3) \leq 9$$

$$-3 \leq \frac{1}{2}x + \frac{3}{2} \leq 9$$

$$\frac{-3}{2} \quad \frac{-3}{2} \quad \frac{-3}{2}$$

$$-4\frac{1}{2} \leq \frac{1}{2}x \leq 7\frac{1}{2}$$

$$-9 \leq x \leq 15 \quad [-9, 15]$$



Name _____

4. Solve and Graph your solution set. Write Your Solution Set in Interval Notation

$$4\frac{1}{5}x + 48 \leq x \quad \text{or} \quad \frac{x+5}{4} < 2(x+12)$$

$$\frac{5}{16} \cdot \frac{16}{5}x \leq -48 \cdot \frac{5}{16}$$

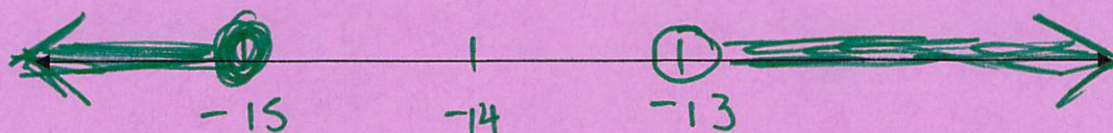
$$x+5 < 8(x+12)$$

$$x+5 < 8x+96$$

$$x \leq -15 \quad \text{or}$$

$$\frac{-7x}{-7} < \frac{91}{-7}$$

$$(-\infty, -15] \cup (-13, \infty) \quad x > -13$$



White: Literal Inequalities

Name _____

1. Solve for x when $p < 0$ and b and g are both positive integers.

$$\frac{bx + gx}{p} > m$$

Name _____

2. Solve for m when $g < 0$

$$\frac{wh - gm}{3} \geq t$$

Name _____

3. Solve for r

$$A > \frac{1}{3}\pi r^2 h$$

Name _____

Solve for y when $x < b$

$$xy < by - t$$

White: Literal Inequalities

Name Key

1. Solve for x when $p < 0$ and b and g are both positive integers.

$$p \cdot \frac{bx + gx}{p} > m \cdot p$$

$$bx + gx < mp$$

$$\frac{x(b+g)}{(b+g)} < \frac{mp}{(b+g)}$$

$$x < \frac{mp}{(b+g)}$$

Name _____

2. Solve for m when $g < 0$

$$3 \cdot \frac{wh - gm}{3} \geq t \cdot 3$$

$$\begin{array}{ccc} wh - gm & \geq & 3t \\ -wh & & -wh \end{array}$$

$$g < 0$$

↓

$$-(-g)$$

This will
be
positive

$$\begin{array}{ccc} -gm & \geq & 3t - wh \\ -g & & -g \end{array}$$

$$m \geq \frac{3t - wh}{-g}$$

Name _____

3. Solve for r

$$3. A > \frac{1}{3} \pi r^2 h \cdot 3$$

$$\frac{3A}{\pi h} > \frac{\pi r^2 h}{\pi h}$$

$$\sqrt{\frac{3A}{\pi h}} > \sqrt{r^2}$$

$$\boxed{\sqrt{\frac{3A}{\pi h}} > r}$$

Name _____

Solve for y when $x < b$

$$xy < by - t$$

$$-by -by$$

$$xy - by < -t$$

$$y(x-b) < -t$$

$$\boxed{y > \frac{-t}{(x-b)}}$$

Orange: Sets

Name _____

1. Set $A = \{x \mid x \text{ is a factor of } 32\}$
Set $B = \{2, 4, 6, 8, 10\}$

(a) Find the intersection of A and B .

(b) Find the union of A and B .

2. If the universal set, $U = \{\text{January, February, March, April, May, June, July, August, September, October, November, December}\}$ and $A = \{\text{January, June, September, October}\}$, write the complement of A .

Name _____

1. Set $A = \{x \mid x \text{ is a factor of } 16\}$
Set $B = \{x \mid x \text{ is a factor of } 24\}$

(a) Find the intersection of A and B .

(b) Find the union of A and B .

2. If the universal set, $U = \{\text{Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday}\}$ and $A = \{\text{Saturday, Sunday}\}$, write the complement of A .

Name _____

1. Set $A = \{x \mid x \text{ is a factor of } 42\}$

Set $B = \{1, 3, 5, 7, 9\}$

(a) Find the intersection of A and B .

(b) Find the union of A and B .

2. If the universal set, $U = \{\text{apple, coconut, peach, blueberry, cherry, strawberry}\}$ and $A = \{\text{apple, coconut, blueberry, cherry}\}$, write the complement of A .

Name _____

1. Set $A = \{1, 3, 5, 7, 9\}$

Set $B = \{2, 4, 6, 8, 10\}$

(a) Find the intersection of A and B .

(b) Find the union of A and B .

2. If the universal set, $U = \{\text{soccer, basketball, football, lacrosse, hockey, golf, cheerleading}\}$ and $A = \{\text{lacrosse, hockey, golf}\}$, write the complement of A .

Orange: Sets

Name Key

1. Set $A = \{x \mid x \text{ is a factor of } 32\} \longrightarrow \{1, 2, 4, 8, 16, 32\}$
Set $B = \{2, 4, 6, 8, 10\}$

(a) Find the intersection of A and B .

$$A \cap B = \{2, 4, 8\}$$

(b) Find the union of A and B .

$$A \cup B = \{1, 2, 4, 6, 8, 10, 16, 32\}$$

2. If the universal set, $U = \{\text{January, February, March, April, May, June, July, August, September, October, November, December}\}$ and $A = \{\text{January, June, September, October}\}$, write the complement of A .

$$A' = \{\text{February, March, April, May, July, August, November, December}\}$$

Name Key

1. Set $A = \{x \mid x \text{ is a factor of } 16\} \longrightarrow \{1, 2, 4, 8, 16\}$
Set $B = \{x \mid x \text{ is a factor of } 24\} \longrightarrow \{1, 2, 3, 4, 6, 8, 12, 24\}$

(a) Find the intersection of A and B .

$$A \cap B = \{1, 2, 4, 8\}$$

(b) Find the union of A and B .

$$A \cup B = \{1, 2, 3, 4, 6, 8, 12, 16, 24\}$$

2. If the universal set, $U = \{\text{Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday}\}$ and $A = \{\text{Saturday, Sunday}\}$, write the complement of A .

$$A' = \{\text{Monday, Tuesday, Wednesday, Thursday, Friday}\}$$

Name Key

1. Set $A = \{x \mid x \text{ is a factor of } 42\} \rightarrow \{1, 2, 3, 6, 7, 12, 21, 42\}$
Set $B = \{1, 3, 5, 7, 9\}$

(a) Find the intersection of A and B .

$$A \cap B = \{1, 3, 7\}$$

(b) Find the union of A and B .

$$A \cup B = \{1, 2, 3, 5, 6, 7, 9, 12, 21, 42\}$$

2. If the universal set, $U = \{\text{apple, coconut, peach, blueberry, cherry, strawberry}\}$ and $A = \{\text{apple, coconut, blueberry, cherry}\}$, write the complement of A .

$$A' = \{\text{peach, strawberry}\}$$

Name Key

1. Set $A = \{1, 3, 5, 7, 9\}$
Set $B = \{2, 4, 6, 8, 10\}$

(a) Find the intersection of A and B .

$$A \cap B = \emptyset$$

(b) Find the union of A and B .

$$A \cup B = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$

2. If the universal set, $U = \{\text{soccer, basketball, football, lacrosse, hockey, golf, cheerleading}\}$ and $A = \{\text{lacrosse, hockey, golf}\}$, write the complement of A .

$$A' = \{\text{soccer, basketball, football, cheerleading}\}$$